## Original Contribution

# THE RATIO BETWEEN THE LENGTH OF UPPER AND DOWN PARTS OF THE BODY IN THE CROSS-SECTION OF THE EQUAL TORQUES APPEARS AS AN ANATOMICAL CONSTANT 

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#### Abstract

The bed scales determine the section, in which the torques of the upper and the down body parts are balanced. In this section the length and mass of the upper and down parts of the body were measured. Aim of the study: To investigate the ratio between the length of the upper and down part of the body in the cross-section of the equal torques of the upper and the down bodily parts. Results: 62 people between the ages of 18 and 28 were examined. The ratio $\mathrm{H}_{\mathrm{up}} / \mathrm{H}_{\text {down }}$ in the cross-section of the equal torques of the upper and down bodily parts don't depend from body height H and is equals to: $\mathrm{H}_{\mathrm{up}} / \mathrm{H}_{\text {down }}=0.791 \mathrm{H}$ (i.e. $\mathrm{H}_{\mathrm{up}}$ $\left./ \mathrm{H}_{\text {down }} \sim 0.8 \mathrm{H}\right)$. Conclusions: The ratio between the length of upper and down parts of the body in the crosssection of the equal torques of upper and lower bodily parts appears nearly an anatomical constant.


Key words: body, mass center, height, BMI, torques.

## INTRODUCTION

In the previous study Atanasov [1, 2] developed a method for measuring the mass-center of the human body using a BED-SCALES device (Figure 1).

The bed-scales determine the section, in which the torques of the upper and down part of the body are balanced in the section O-O'. In this section, the body circumference is measured and a connection is sought between the measured body circumference and the parameters - body weight ( $\mathrm{M}, \mathrm{kg}$ ), body height ( $\mathrm{H}, \mathrm{m}$ ), and body mass index ( $\mathrm{BMI}, \mathrm{kg} / \mathrm{m}^{2}$ ). Indeed, Figure 1 shows that:
$\mathrm{G}_{\text {up }} \mathrm{H}_{\text {up }}=\mathrm{G}_{\text {down }} \mathrm{H}_{\text {down }}$
$\mathrm{H}=\mathrm{H}_{\text {up }}+\mathrm{H}_{\text {down }}$
$\mathrm{G}=\mathrm{G}_{\text {up }}+\mathrm{G}_{\text {down }}$
Where $G, G_{\text {up }}$ and $G_{\text {down }}$ are the mass of the whole body of the upper body, and of the down body respectively. $\mathrm{H}, \mathrm{H}_{\text {up }}$ and $\mathrm{H}_{\text {down }}$ are the height of the whole body and the upper and the down part of the body, respectively. The
products $\mathrm{G}_{\mathrm{up}} \mathrm{H}_{\text {up }}$ and $\mathrm{G}_{\text {down }} \mathrm{H}_{\text {down }}$ are the torques of the upper and down body parts.

In the section $\mathrm{O}-\mathrm{O}^{\prime}$ ', in which the torques GupHup and Gdown Hdown are equal, the circumference of the body $L$ is measured, with the help of which the center of gravity of the body is determined.

From $G_{\text {up }}$ and $G_{\text {down }}$ it can calculate the mass of the upper and down part of the body:

$$
\begin{array}{ll}
M_{u p}=G_{u p} / g & \text { (4) } \\
M_{\text {down }}=G_{\text {down }} / g & \text { and } \\
\text { (5), where }
\end{array}
$$

$$
\mathrm{g} \text { is the Earth acceleration }\left(\mathrm{g}=9.81 \mathrm{~m} / \mathrm{s}^{2}\right) \text {. }
$$

Thus, the ratio (1) gives the form of:

| $M_{u p} g H_{u p}=M_{\text {down }} g H_{\text {down }}$ | (6) | or |
| :--- | :--- | ---: |
| $M_{u p} H_{\text {up }}=M_{\text {down }} H_{\text {down }}$ | (7) | and |
| $H_{\text {up }} / H_{\text {down }}=M_{\text {down }} / M_{\text {up }}$ | (8) |  |

## AIM OF THE STUDY

To investigate the ratio between the length of upper and down parts of the body in the cross section of the equal torques of the upper and the down bodily parts:

1. Measure the mass of the body M , the height H of body, $\mathrm{H}_{\mathrm{up}}$, and $\mathrm{H}_{\text {down }}$ length, $\mathrm{M}_{\text {down }}$ and
$\mathrm{M}_{\mathrm{up}}$ mass in the cross section of the equal torques.
2. Calculate the body mass index (BMI).
3. Calculate $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}$ and $\mathrm{M}_{\text {down }} / \mathrm{M}_{\text {up }}$ ratio.
4. Investigate the statistical relationship between the measured parameters.


Figure 1. Bed-scales device. $\mathrm{H}_{\mathrm{up}}$ and $\mathrm{H}_{\text {down }}$ length were measured in the cross-section OO' of the equal torques of upper and down bodily parts.

## MATERIALS AND METHODS

62 people aged between 18 and 28 of both sexes were studied ( 24 men against 40 women).
The statistical program STATISTICS is used in the calculations.
The statistical significance of the found correlations was determined using Student's ttest.

## RESULTS

The measured parameters - body weight M, body height $\mathrm{H}, \mathrm{H}_{\text {up }}, \mathrm{H}_{\text {down }}$, calculated BMI and $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}$ values are given in Table 1. From the ratio (8) it can see that $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}$ ratio is equals to $\mathrm{M}_{\text {down }} / \mathrm{M}_{\text {up }}$ ratio, because of that the $\mathrm{M}_{\text {down }} / \mathrm{M}_{\mathrm{up}}$ values are not given in Table 1.

Table 1. Body mass $M$, body height H, BMI, $H_{u p}, H_{\text {down }}$, and calculated $H_{u p} / H_{\text {down }}$ ratio*.
Gender of participants are signed as ( $m$ ) man and (w) woman.

| N | $\mathrm{M}(\mathrm{kg})$ | $\mathrm{H}(\mathrm{m})$ | BMI $\left(\mathrm{kg} / \mathrm{m}^{2}\right)$ | $\mathrm{H}_{\text {up }}(\mathrm{m})$ | $\mathrm{H}_{\text {down }}(\mathrm{m})$ | $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | $75(\mathrm{~m})$ | 1.87 | 21.44 | 0.82 | 1.050 | 0.78095 |
| 2 | $44(\mathrm{w})$ | 1.60 | 17.1875 | 0.71 | 0.89 | 0.79775 |
| 3 | $102(\mathrm{~m})$ | 1.84 | 30.1275 | 0.82 | 1.020 | 0.8039 |
| 4 | $97(\mathrm{~m})$ | 1.83 | 28.9647 | 0.82 | 1.010 | 0.81188 |
| 5 | $57.9(\mathrm{w})$ | 1.57 | 23.4897 | 0.70 | 0.87 | 0.80459 |
| 6 | $54.4(\mathrm{w})$ | 1.55 | 22.64 | 0.71 | 0.84 | 0.84523 |
| 7 | $70(\mathrm{~m})$ | 1.74 | 23.12 | 0.75 | 0.99 | 0.7575 |
| 8 | $59.3(\mathrm{w})$ | 1.75 | 19.36 | 0.79 | 0.96 | 0.82251 |
| 9 | $64.8(\mathrm{w})$ | 1.74 | 21.40 | 0.79 | 0.95 | 0.83157 |
| 10 | $69.7(\mathrm{~m})$ | 1.64 | 25.9 | 0.70 | 0.94 | 0.7446 |
| 11 | $56(\mathrm{w})$ | 1.65 | 20.57 | 0.77 | 0.88 | 0.8750 |
| 12 | $64(\mathrm{~m})$ | 1.83 | 19.11 | 0.78 | 1.050 | 0.7428 |
| 13 | $52.1(\mathrm{w})$ | 1.66 | 18.906 | 0.77 | 0.925 | 0.8324 |
| 14 | $63.9(\mathrm{w})$ | 1.66 | 23.189 | 0.69 | 0.97 | 0.71134 |
| 15 | $103(\mathrm{~m})$ | 1.7 | 35.64 | 0.73 | 0.97 | 0.7525 |

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| 16 | $66.6(\mathrm{w})$ | 1.7 | 23 | 0.76 | 0.94 | 0.8085 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 17 | $73.5(\mathrm{~m})$ | 1.8 | 22.685 | 0.79 | 1.02 | 0.7745 |
| 18 | $51(\mathrm{w})$ | 1.69 | 17.857 | 0.76 | 0.93 | 0.8172 |
| 19 | $43.8(\mathrm{w})$ | 1.56 | 17.998 | 0.68 | 0.88 | 0.7727 |
| 20 | $67.3(\mathrm{w})$ | 1.73 | 22.485 | 0.77 | 0.96 | 0.80208 |
| 21 | $63(\mathrm{~m})$ | 1.78 | 19.88 | 0.80 | 0.98 | 0.8163 |
| 22 | $63.5(\mathrm{w})$ | 1.65 | 23.32 | 0.75 | 0.90 | 0.8333 |
| 23 | $86.5(\mathrm{~m})$ | 1.88 | 24.47 | 0.835 | 1.05 | 0.7952 |
| 24 | $81(\mathrm{~m})$ | 1.83 | 24.187 | 0.87 | 0.97 | 0.8969 |
| 25 | $82(\mathrm{~m})$ | 1.77 | 26.17 | 0.79 | 0.97 | 0.8144 |
| 26 | $95(\mathrm{~m})$ | 1.9 | 26.315 | 0.83 | 1.08 | 0.7685 |
| 27 | $81(\mathrm{~m})$ | 1.78 | 25.564 | 0.78 | 1.00 | 0.78 |
| 28 | $93(\mathrm{~m})$ | 1.75 | 30.367 | 0.71 | 1.04 | 0.6893 |
| 29 | $86(\mathrm{~m})$ | 1.85 | 25.128 | 0.81 | 1.05 | 0.7714 |
| 30 | $73(\mathrm{~m})$ | 1.83 | 21.798 | 0.80 | 1.03 | 0.7767 |
| 31 | $55(\mathrm{w})$ | 1.73 | 18.377 | 0.79 | 0.94 | 0.8404 |
| 32 | $76(\mathrm{~m})$ | 1.88 | 21.50 | 0.84 | 1.04 | 0.8077 |
| 33 | $90(\mathrm{~m})$ | 1.88 | 25.46 | 0.82 | 1.05 | 0.78095 |
| 34 | $50.7(\mathrm{w})$ | 1.59 | 20.05 | 0.70 | 0.89 | 0.7865 |
| 35 | $74(\mathrm{w})$ | 1.6 | 28.906 | 0.71 | 0.88 | 0.8068 |
| 36 | $58(\mathrm{w})$ | 1.55 | 24.14 | 0.70 | 0.86 | 0.81395 |
| 37 | $88(\mathrm{~m})$ | 1.74 | 29.065 | 0.76 | 0.98 | 0.7755 |
| 38 | $60(\mathrm{w})$ | 1.64 | 22.30 | 0.69 | 0.96 | 0.71875 |
| 39 | $110(\mathrm{~m})$ | 1.81 | 33.57 | 0.81 | 1.0 | 0.81 |
| 40 | $56(\mathrm{w})$ | 1.54 | 23.61 | 0.68 | 0.87 | 0.7816 |
| 41 | $95(\mathrm{~m})$ | 1.79 | 29.65 | 0.75 | 1.04 | 0.7211 |
| 42 | $54(\mathrm{w})$ | 1.70 | 18.685 | 0.74 | 0.96 | 0.7708 |
| 43 | $54(\mathrm{w})$ | 1.7 | 18.685 | 0.74 | 0.96 | 0.7708 |
| 44 | $54(\mathrm{w})$ | 1.59 | 21.36 | 0.70 | 0.90 | 0.7777 |
| 45 | $55(\mathrm{w})$ | 1.60 | 21.484 | 0.70 | 0.90 | 0.7777 |
| 46 | $59.5(\mathrm{w})$ | 1.63 | 22.394 | 0.73 | 0.90 | 0.81111 |
| 47 | $104(\mathrm{~m})$ | 1.8 | 32.1 | 0.74 | 1.05 | 0.7047 |
| 48 | $63(\mathrm{w})$ | 1.68 | 22.32 | 0.77 | 0.92 | 0.83695 |
| 49 | $75.5(\mathrm{~m})$ | 1.84 | 22.287 | 0.77 | 1.06 | 0.7264 |
| 50 | $55(\mathrm{w})$ | 1.72 | 18.591 | 0.76 | 0.96 | 0.7917 |
| 51 | $67(\mathrm{w})$ | 1.70 | 23.18 | 0.76 | 0.94 | 0.8085 |
| 52 | $57(\mathrm{w})$ | 1.65 | 20.936 | 0.73 | 0.93 | 0.7849 |
| 53 | $83(\mathrm{w})$ | 1.60 | 32.422 | 0.68 | 0.91 | 0.74725 |
| 54 | $52(\mathrm{w})$ | 1.54 | 21.93 | 0.71 | 0.83 | 0.8554 |
| 55 | $47(\mathrm{w})$ | 1.64 | 17.475 | 0.77 | 0.87 | 0.885 |
| 56 | $54(\mathrm{w})$ | 1.63 | 20.32 | 0.72 | 0.92 | 0.7826 |
| 57 | $90(\mathrm{w})$ | 1.62 | 34.293 | 0.73 | 0.89 | 0.8202 |
| 58 | $60(\mathrm{w})$ | 1.5 | 26.66 | 0.66 | 0.85 | 0.7764 |
| 59 | $59(\mathrm{w})$ | 1.65 | 21.671 | 0.72 | 0.94 | 0.7595 |
| 60 | $62(\mathrm{w})$ | 1.63 | 23.335 | 0.72 | 0.91 | 0.7912 |
| 61 | $51(\mathrm{w})$ | 1.54 | 21.5 | 0.68 | 0.87 | 0.7816 |
| 62 | $47(\mathrm{w})$ | 1.58 | 18.827 | 0.70 | 0.87 | 0.8046 |
|  | 7 |  |  |  |  |  |

[^0]A parametric linear regression analysis of the statistical relationship between the body parameters ( $\mathrm{a}, \mathrm{b}, \mathrm{c}$ ) was performed:
a. $\left(\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}\right)$ ratio and body height $(\mathrm{H})$ of the subjects - Figure 2.
b. $\left(\mathrm{H}_{\mathrm{up}} / \mathrm{H}_{\text {down }}\right)$ ratio and body mass $(\mathrm{M})$ of the subjects - Figure 3.
c. $\left(\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}\right)$ ratio and body mass index (BMI) of the subjects-Figure 4.

Table 2 presents the studied dependencies and their correlation coefficients.


Figure 2. Relationship between $\mathrm{H}_{\mathrm{up}} / \mathrm{H}_{\text {down }}$ and body height H .


Figure 3. Relationship between $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}$ and body mass M .
Table 2. The studied bodily dependencies and their correlation coefficients

| Measured values | Statistical relationship | Correlation <br> coefficients | (Statistical - <br> significance $)$ |
| :--- | :--- | :--- | :--- |
| 1). $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}-\mathrm{H}$ | $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}=-0.0465 \mathrm{H}+0.8716$ | $\mathrm{R}=-0.11$ | $(\mathrm{p}>0.05)$ |
| 2). $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}-\mathrm{M}$ | $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}=-0.0008 \mathrm{M}+0.8451$ | $\mathrm{R}=-0.29$ | $(\mathrm{p}<0.05)$ |
| 3). $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}-\mathrm{BMI}$ | $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}=-0.0031$ BMI +0.8666 | $\mathrm{R}=-0.31$ | $(\mathrm{p}<0.05)$ |
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From experimental data on Table 2 and Figure 2 it can see that the ratio $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}$ in the cross section of the equal torques of the upper and lower bodily parts don't depend from body height H . The correlation coefficient between $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}$ and H (see Eq. 1 ) is very low $\quad(\mathrm{R}=-$ 0.11 ) and the connection between two quantities do not have statistical significance ( $\mathrm{p}>0.05$ ).

The calculated $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}$ ratio of 62 persons fall in the range of $0.75-0.832$ with mean ( $\pm \mathrm{SD}$ ) equals to $0.791( \pm 0.041)$. Independently to the body height, the body mass and the body-mass index this, this ratio remains constantly: $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}=0.791 \mathrm{H}$.

Because of $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}=\mathrm{M}_{\text {down }} / \mathrm{M}_{\mathrm{up}}$, the ratio between the down and the upper body mass in the cross section of the equal torques is equals to: $\mathrm{M}_{\text {down }} / \mathrm{M}_{\mathrm{up}}=0.791 \mathrm{H}$.

From experimental data on Table 2 and Figure 3, and Figure 4 is observed that the relationship $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}$ depends slightly from the body mass M (Eq. 2 ) and the body mass index BMI (Eq.3). In the two cases the correlation coefficients $\mathrm{R}=-0.29$ and $\mathrm{R}=-$ 0.31 are low, but the connection between $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}$ and M , and BMI have a statistically significance ( $\mathrm{p}<0.05$ ).


Figure 4. Relationship between $\mathrm{H}_{\mathrm{up}} / \mathrm{H}_{\text {down }}$ and BMI.


Figure 5. The approximate location of the cross section of the equal torques of the upper and lower part of the human body: Hup / Hdown ~ 8/10.

## DISCUSSION

The ratio $\mathrm{H}_{\mathrm{up}} / \mathrm{H}_{\text {down }}$ remains constantly, independently to the gender, the body height, the body mass and the body-mass index: $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}=0.791 \mathrm{H}\left(/\right.$ i.e. $\left.\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }} \sim 0.8 \mathrm{H}\right)$.

Because of $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}=\mathrm{M}_{\text {down }} / \mathrm{M}_{\text {up }}$, the ratio between the down and the upper body parts of the mass in the cross section of the equal torques is
equals to: $\mathrm{M}_{\text {down }} / \mathrm{M}_{\mathrm{up}}=0.791 \mathrm{H}$ (i.e. $\mathrm{M}_{\text {down }} / \mathrm{M}_{\mathrm{up}}$ $\sim 0.8 \mathrm{H}$ ).

On Figure 5 is shown the approximate location of the cross section of the equal torques of the body.

The find relationships can be used to solve various scientific problems such as abdominal obesity, spinal deformities and others [3-6].

## CONCLUSSION

The ratio between the length of $\mathrm{H}_{\text {up }}$ and $\mathrm{H}_{\text {down }}$ part of the body in the cross section of the equal torques of upper and lower bodily parts appears nearly an anatomical constant. This ratio can be presented as $\mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }} \sim 8 / 10$.

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[^0]:    $* \mathrm{H}_{\text {up }} / \mathrm{H}_{\text {down }}=\mathrm{M}_{\text {down }} / \mathrm{M}_{\text {up }}$

